

# Grain growth of ZnO in binary ZnO-V<sub>2</sub>O<sub>5</sub> ceramics

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Grain growth of ZnO during liquid-phase sintering of binary ZnO-V<sub>2</sub>O<sub>5</sub> ceramics has been studied for V<sub>2</sub>O<sub>5</sub> contents from 0.5 to 4 mol% and sintering from 900°C to 1200°C. The results are discussed and compared with previous studies in terms of the phenomenological kinetic grain growth expression:

$$G^n - G_0^n = K_0 t \exp(-Q/RT).$$

Addition of V<sub>2</sub>O<sub>5</sub> is found to decrease the ZnO grain growth exponent,  $n$ , as well as the apparent activation energy,  $Q$ . The activation analysis also reveals a change in the rate-controlling mechanism for ZnO grain growth. Following a low-V<sub>2</sub>O<sub>5</sub>-content ( $\leq 2$  mol%) of nearly constant  $Q$  values of about 88 kJ/mol, further V<sub>2</sub>O<sub>5</sub> additions cause an increase of the  $Q$  value to about 115 kJ/mol. Consistent with accepted models of liquid-phase sintering, it is concluded that the rate-controlling mechanism of ZnO grain growth during liquid-phase sintering in the presence of V<sub>2</sub>O<sub>5</sub> changes from one of a phase-boundary reaction at low V<sub>2</sub>O<sub>5</sub> levels to one of diffusion through the liquid phase at more than 2 mol% V<sub>2</sub>O<sub>5</sub> levels. © 2003 Kluwer Academic Publishers

## 1. Introduction

Zinc oxide ceramic varistors derive their non-linear current-voltage behaviour from the addition of small amounts of other metal oxides, such as Bi<sub>2</sub>O<sub>3</sub>, Pr<sub>6</sub>O<sub>11</sub>, MnO<sub>2</sub> and Co<sub>3</sub>O<sub>4</sub> [1–7]. Until recently, it was believed that effective varistor-forming ingredients were heavy elements with large ionic radii, such as bismuth [2, 3], praseodymium [4, 5], and barium [6, 7], but studies have now shown that the ZnO-V<sub>2</sub>O<sub>5</sub> system also exhibits varistor behaviour [8–17]. This system is of interest because the ceramic can be sintered at a relatively low temperature of about 900°C. This is important for applications in which it can be a multi-layered chip component, because it can be co-fired with a silver inner-electrode (m.p. 961°C) without using the expensive palladium or platinum metals.

Electrical properties of these ZnO ceramic varistors are directly dependent on the microstructure as the ZnO grain size affects the varistor breakdown voltage per unit thickness [1–7]. There have been a number of studies addressing the sintering and grain growth of pure ZnO [18, 19] and the ZnO-Bi<sub>2</sub>O<sub>3</sub> ceramic system [20–22], as it is important to fundamentally understand the microstructural development of ZnO ceramics. Although there have been studies investigating the grain growth phenomenon in ZnO with V<sub>2</sub>O<sub>5</sub> additions [10], activation analyses of grain growth have not been attempted. Other than our preliminary report on a ZnO-1 mol% V<sub>2</sub>O<sub>5</sub> ceramic [23], the role of V<sub>2</sub>O<sub>5</sub>-rich phase as it affects the grain growth kinetics of ZnO has not been quantitatively documented. In view that V<sub>2</sub>O<sub>5</sub>-

doped ZnO varistors have the potential of replacing Bi<sub>2</sub>O<sub>3</sub>-doped ZnO varistors due to its low sintering temperature, a detailed analytical study of the ZnO grain growth in the ZnO-V<sub>2</sub>O<sub>5</sub> ceramic system has to be done.

Hence, in this work, we will address the effects of V<sub>2</sub>O<sub>5</sub> additions (0.5 to 4 mol%) in a quantitative manner by using an activation analysis of the kinetic parameters of ZnO grain growth, specifically the kinetic grain-growth exponent and the apparent activation energy for grain growth. These parameters are obtained from the phenomenological kinetic grain growth equation [21, 22]:

$$G^n - G_0^n = K_0 t \exp(-Q/RT) \quad (1)$$

where  $G$  is the average grain size at time  $t$ , the  $n$  value is the kinetic grain growth exponent,  $K_0$  is the pre-exponential constant of the material,  $Q$  is the apparent activation energy,  $R$  is the universal gas constant, and  $T$  is the absolute temperature. In this study, the initial grain size,  $G_0$ , is significantly smaller than the grain size,  $G$ , at some later time. Thus,  $G_0$  can be neglected, and Equation 1 simplifies to

$$G^n = K_0 t \exp(-Q/RT) \quad (2)$$

which will be used throughout this study.

## 2. Experimental procedures

High purity oxide powder starting materials were used for the preparation of the ZnO-V<sub>2</sub>O<sub>5</sub> samples. Four

compositions, 0.5, 1, 2 and 4 mol%  $V_2O_5$  were investigated. The powder mixtures were ball-milled for 24 hrs using alumina balls in deionised water. The mixtures were filtered, dried and pressed into pellets of 13 mm diameter and 3 mm thickness. The pellets were then sintered at four temperatures (900, 1000, 1100 and 1200°C) for 4 hrs. Another series of specimens are sintered at 900°C for five different times (0.5, 1, 2, 4 and 8 hrs). Heating and cooling rates of 5°C/min were used. According to the ZnO- $V_2O_5$  phase diagram [24, 25], ZnO has a eutectic reaction with  $Zn_3(VO_4)_2$  at ~890°C. Thus, sintering temperatures  $\geq 900^\circ\text{C}$  were chosen in this study to ensure that the vanadium-rich liquid phase will enhance the densification of the samples. Densities were calculated from the weights and dimensions of the ceramic bodies.

Microstructures of the samples were observed using a scanning electron microscope (JEOL JSM-5310) operated at 20 kV. The sintered specimens were cut diametrically using low speed diamond saw, and mounted with conductive resin. The samples were then ground with 600–1000 grit SiC paper, and finally polished to 1  $\mu\text{m}$  surface finish using diamond paste. The surface were etched with 2% nital for about 1 min. Grain sizes were measured directly from the micrographs of the etched samples by the linear intercept technique described by Mendelson [26]. The average grain size,  $G$ , was obtained as

$$G = 1.56 \bar{L} \quad (3)$$

where  $\bar{L}$  is the average grain-boundary intercept length of a series of random lines on the micrographs.

### 3. Results

#### 3.1. Density

Relative densities of the various ZnO- $V_2O_5$  samples sintered at different temperatures and times are shown in Fig. 1. Densities of the four systems remained rather constant over the range of sintering times studied (Fig. 1a). However, the relative density decreased with increasing sintering temperature (Fig. 1b), which is most probably due to volatility of  $V_2O_5$  at high temperature. This was also observed by Tsai and Wu [9] in their ZnO- $V_2O_5$  binary systems.

#### 3.2. Microstructural observations

Microstructural features of all the sintered ZnO- $V_2O_5$  samples are similar, except for the average ZnO grain size. They showed the following features: (1) large grains dispersed in a matrix composed of small grains and (2) the large grains having oblong shape. Such exaggerated ZnO grain growth was often found in  $V_2O_5$ -doped ZnO ceramics [8–17]. It was the high reactivity of the vanadium-rich liquid phase during sintering which caused such abnormal grain growth. However, the microstructure becomes more uniform as sintering temperature and time increases.

Microstructures of the series of ZnO- $V_2O_5$  ceramics sintered at 900°C for 8 hrs are illustrated in Fig. 2. The average ZnO grain size initially increases with increasing  $V_2O_5$  content up to 2 mol%. A further increase

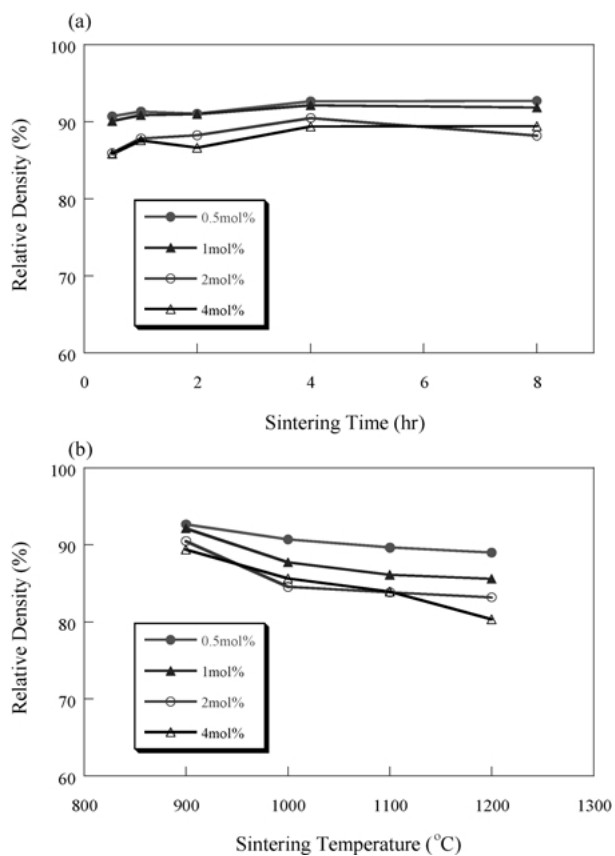


Figure 1 Effect of sintered density of ZnO- $V_2O_5$  samples with (a) sintering time (sintered at 900°C) and (b) sintering temperature (sintered for 4 hrs).

of  $V_2O_5$  content to  $>2$  mol% causes a decrease in the grain size (Fig. 3). Tsai and Wu [9] also reported a similar trend for the effect of  $V_2O_5$  on the grain growth of ZnO. They reported that ZnO grain growth is enhanced over that of pure ZnO with only a 0.25 mol% addition of  $V_2O_5$ , and observed a reduction of grain size at 2 mol%  $V_2O_5$ . However, they did not complete an activation analysis to identify the rate-controlling mechanism. It is reasonable to expect that this change in trend of the final grain size may correspond to a transition in the rate-controlling mechanism of the ZnO grain growth.

#### 3.3. Activation analysis of kinetic grain-growth parameters

The phenomenological kinetic grain growth equation given by Equation 2 can be readily plotted in the form:

$$\log G = \frac{1}{n} \log t + \frac{1}{n} \left[ \log K_0 - 0.434 \left( \frac{Q}{RT} \right) \right] \quad (4)$$

From the slope of the  $\log G$  versus  $\log t$  line, which is  $1/n$ , the grain growth kinetic exponent  $n$  is readily determined. Fig. 4 illustrates the isothermal grain growth results for the various ZnO- $V_2O_5$  samples sintered at 900°C in the form of Equation 4. The  $n$  value varies with  $V_2O_5$  content, as summarised in Table I. Samples containing 0.5, 1 and 2 mol%  $V_2O_5$  content have similar  $n$  values ranging between 1.5 to 1.8, while sample containing 4 mol%  $V_2O_5$  has a higher  $n$  value of 2.69. Our previous work [23] on ZnO-1 mol%  $V_2O_5$  showed a  $n$

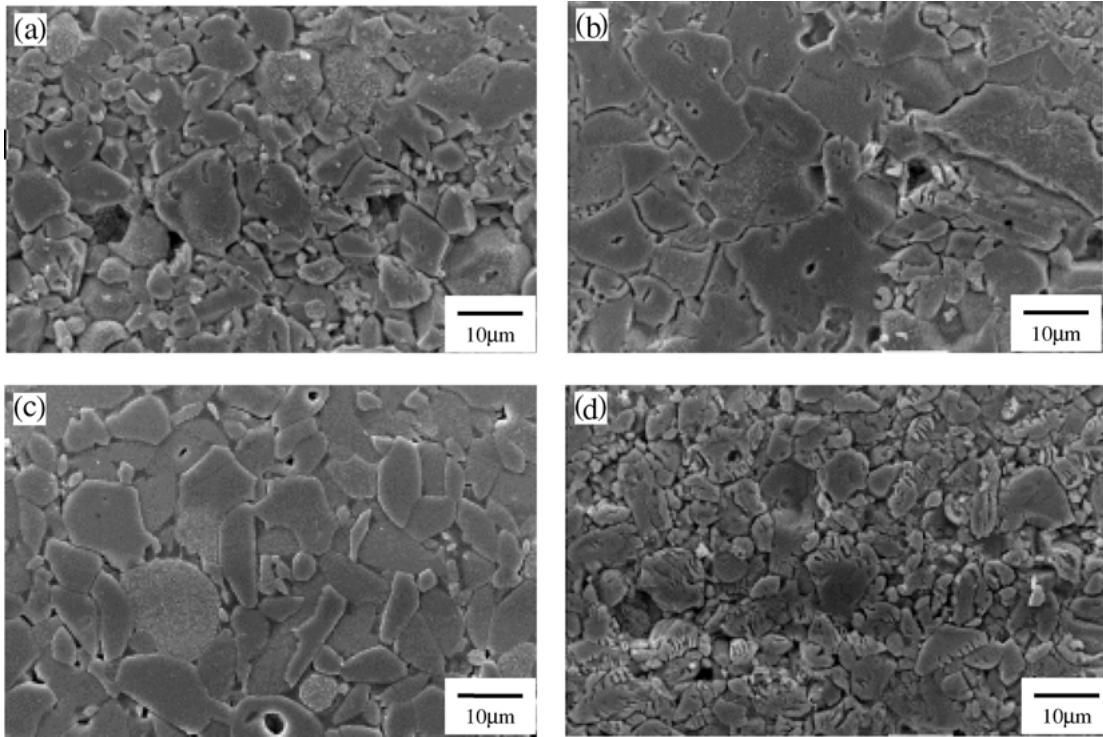


Figure 2 Microstructures in the ZnO-V<sub>2</sub>O<sub>5</sub> systems sintered at 900°C for 8 hrs: (a) 0.5 mol% V<sub>2</sub>O<sub>5</sub>, (b) 1 mol% V<sub>2</sub>O<sub>5</sub>, (c) 2 mol% V<sub>2</sub>O<sub>5</sub>, and (d) 4 mol% V<sub>2</sub>O<sub>5</sub>.

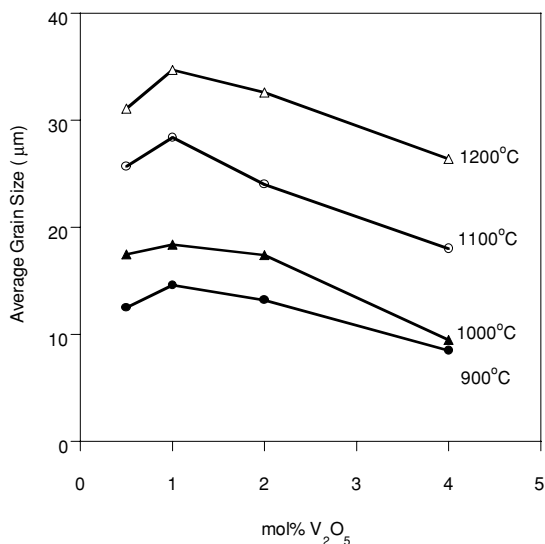


Figure 3 Average ZnO grain size versus V<sub>2</sub>O<sub>5</sub> content (in mol%) for samples sintered in air for 4 hrs.

value of 1.44, which is very close to the value of 1.52 obtained in this study. Moreover, our result also agrees well with Tsai and Wu [9], who obtained  $1/n$  values ranging from 0.63 to 0.83 (equivalent to  $n$  values of 1.20 to 1.59) for 0.5 mol% to 2 mol% V<sub>2</sub>O<sub>5</sub>. The  $n$  values for ZnO-V<sub>2</sub>O<sub>5</sub> systems are lower compared to the value of 3 for pure ZnO [21], indicating V<sub>2</sub>O<sub>5</sub>-doped ZnO has a faster grain growth rate than pure ZnO.

To determine the value of activation energy,  $Q$ , for grain growth, Equation 2 can be expressed as

$$\log\left(\frac{G^n}{t}\right) = \log K_0 - \frac{0.434Q}{R} \left(\frac{1}{T}\right) \quad (5)$$

so that slopes of the Arrhenius plots of  $\log(G^n/t)$  versus  $1/T$  yield values of  $Q$  for grain growth. To compare the values of  $Q$  and  $K_0$  for the four compositions, it is necessary to have the same units for these quantities. As  $n$  has a direct bearing on the units, particularly those of the preexponential term,  $K_0$ , the average  $n$  value of the four compositions ( $n = 2$ ) is used to construct the respective Arrhenius plots (Fig. 5). The activation energies  $Q$  derived from the slopes of the Arrhenius plots are  $90 \pm 6$  kJ/mol for 0.5 mol% V<sub>2</sub>O<sub>5</sub>,  $87 \pm 9$  kJ/mol for 1 mol% V<sub>2</sub>O<sub>5</sub>,  $87 \pm 6$  kJ/mol for 2 mol% V<sub>2</sub>O<sub>5</sub>, and  $115 \pm 24$  kJ/mol for 4 mol% V<sub>2</sub>O<sub>5</sub>. The  $Q$  values are virtually identical for V<sub>2</sub>O<sub>5</sub> content ranging from 0.5–2 mol%, suggesting that the mechanism for ZnO grain growth is identical for all these three V<sub>2</sub>O<sub>5</sub>-containing compositions. At higher V<sub>2</sub>O<sub>5</sub> content, the activation energy is observed to increase, which indicates a change in the grain growth mechanism. It is also worth noting that the  $Q$  values for V<sub>2</sub>O<sub>5</sub>-containing compositions are consistently lower than the activation energy of pure ZnO,  $224 \pm 16$  kJ/mol [21].

From the plots in Fig. 5, it is also possible to estimate the preexponential term,  $K_0$ , in Equation 2. The results of which are summarised in Table I. The preexponential factor contains the concentration of the solid in the liquid, the atomic volume of the solid, the

TABLE I Grain growth parameters

Compositions	$n$	$Q$ (kJ/mol)	$K_0$ ( $\mu\text{m}^2/\text{h}$ )
ZnO-0.5 mol% V <sub>2</sub> O <sub>5</sub>	1.60	$90 \pm 6$	$3.9 \times 10^5$
ZnO-1 mol% V <sub>2</sub> O <sub>5</sub>	1.52	$87 \pm 9$	$3.7 \times 10^5$
ZnO-2 mol% V <sub>2</sub> O <sub>5</sub>	1.79	$87 \pm 6$	$3.0 \times 10^5$
ZnO-4 mol% V <sub>2</sub> O <sub>5</sub>	2.69	$115 \pm 24$	$17.3 \times 10^5$

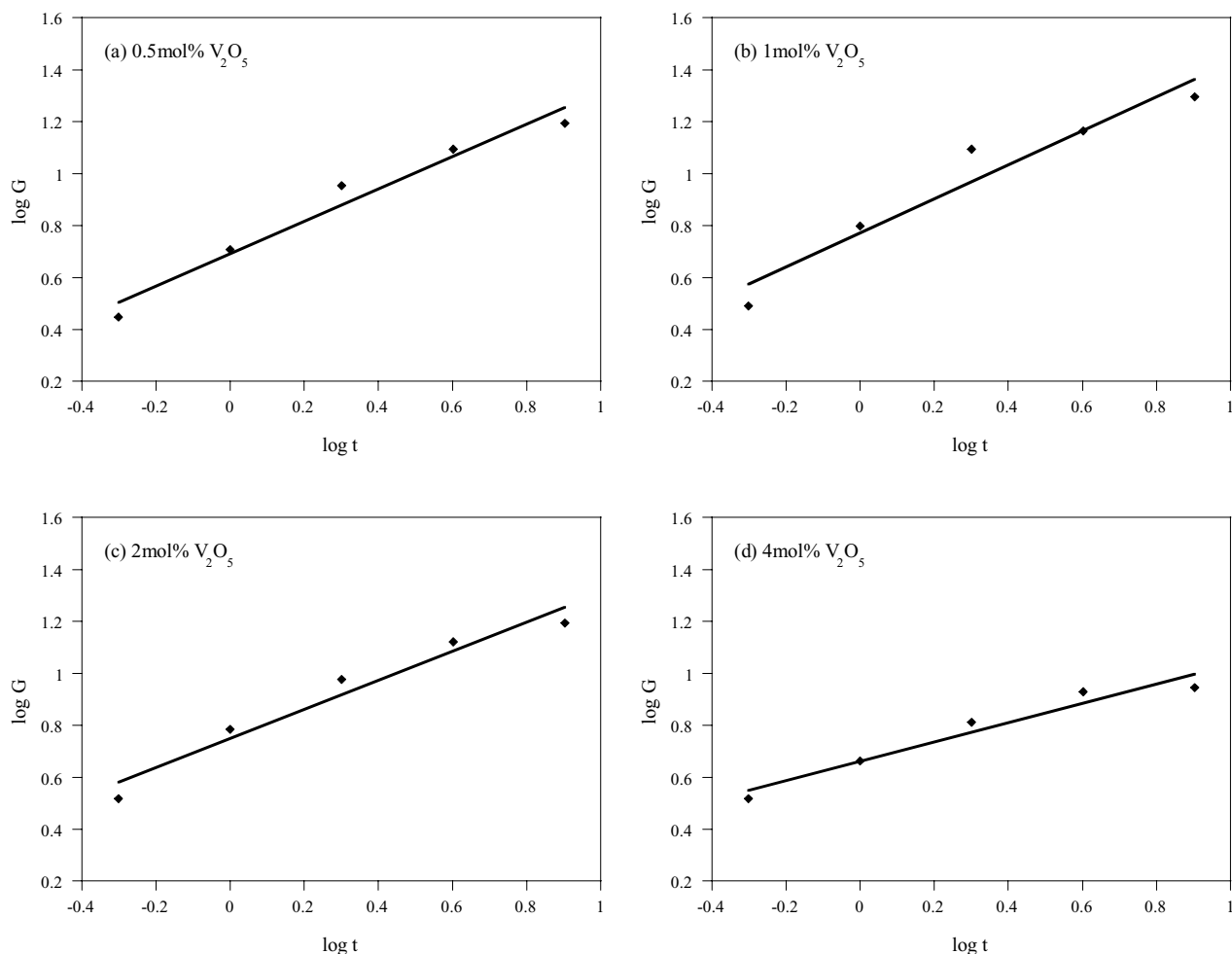


Figure 4 Grain growth of ZnO-V<sub>2</sub>O<sub>5</sub> samples sintered at 900°C for various sintering times: (a) 0.5 mol% V<sub>2</sub>O<sub>5</sub>, (b) 1 mol% V<sub>2</sub>O<sub>5</sub>, (c) 2 mol% V<sub>2</sub>O<sub>5</sub>, and (d) 4 mol% V<sub>2</sub>O<sub>5</sub>.

solid-liquid surface energy, and either the interface reaction rate constant or the diffusivity of the solid through the liquid, depending on the rate controlling process. The  $K_0$  values remain rather constant for V<sub>2</sub>O<sub>5</sub> content up to 2 mol%, and increases significantly with further V<sub>2</sub>O<sub>5</sub> addition to 4 mol%. This further supports the premise that the grain growth mechanism is the same for V<sub>2</sub>O<sub>5</sub> compositions up to 2 mol%, and that a change in the rate controlling process is observed for higher V<sub>2</sub>O<sub>5</sub> content. Unfortunately, the units of the  $K_0$  terms for pure ZnO are not the same as for the V<sub>2</sub>O<sub>5</sub>-containing compositions, so that term cannot be directly compared.

#### 4. Discussion

It has been shown that the rate-controlling grain growth mechanism in pure ZnO involves solid-state diffusion of the Zn<sup>2+</sup> cations within the ZnO lattice, and that the apparent activation energy,  $Q$ , is about  $224 \pm 16$  kJ/mol [21]. Analyses on ZnO-Bi<sub>2</sub>O<sub>3</sub> systems [21, 22] has found that the  $Q$  value decreases significantly with small addition of about 0.5 wt% Bi<sub>2</sub>O<sub>3</sub>, which remains constant up to about 4 wt%, and subsequently increases with further addition of Bi<sub>2</sub>O<sub>3</sub>. It is claimed that the initial decrease in the  $Q$  value is due to the change in the mechanism for ZnO grain growth from solid-state diffusion of Zn<sup>2+</sup> for pure ZnO to solution-precipitation

for the liquid phase sintering in the presence of Bi-rich liquid. As the content of Bi<sub>2</sub>O<sub>3</sub> increases, the thickness of liquid layer also increases. For addition of Bi<sub>2</sub>O<sub>3</sub> up to 4 wt%, the ZnO grain growth rate is controlled by the solution-precipitation phase boundary reaction. Grain growth with this mechanism is independent of the thickness of the liquid layer, and hence, the grain growth rate is not reduced even though the content of Bi<sub>2</sub>O<sub>3</sub> or thickness is increased. However, at higher Bi<sub>2</sub>O<sub>3</sub> content >4 wt%, the mechanism changes to diffusion through the intergranular liquid layer. The grain growth rate is now inversely related to the thickness of the liquid layer between grains. As the thickness of liquid layer increases, the increased diffusion distance through liquid layer reduces the rate of ZnO grain growth, as observed in the increase in the  $Q$  value.

The  $Q$  values of the ZnO-V<sub>2</sub>O<sub>5</sub> systems obtained in this current work vary with the V<sub>2</sub>O<sub>5</sub> content in a similar manner as the ZnO-Bi<sub>2</sub>O<sub>3</sub> system. Initial addition of 0.5 mol% V<sub>2</sub>O<sub>5</sub> decreases  $Q$  significantly. This value remains rather constant up to 2 mol% V<sub>2</sub>O<sub>5</sub>, and increases when V<sub>2</sub>O<sub>5</sub> content is further increased to 4 mol%. Hence, it is possible to postulate that the ZnO grain growth mechanism varies with V<sub>2</sub>O<sub>5</sub> content in a similar way as the ZnO-Bi<sub>2</sub>O<sub>3</sub> system. It changes from solid state diffusion of Zn<sup>2+</sup> for pure ZnO to phase boundary controlled precipitation-solution reaction for V<sub>2</sub>O<sub>5</sub> addition of up to 2 mol%. The mechanism

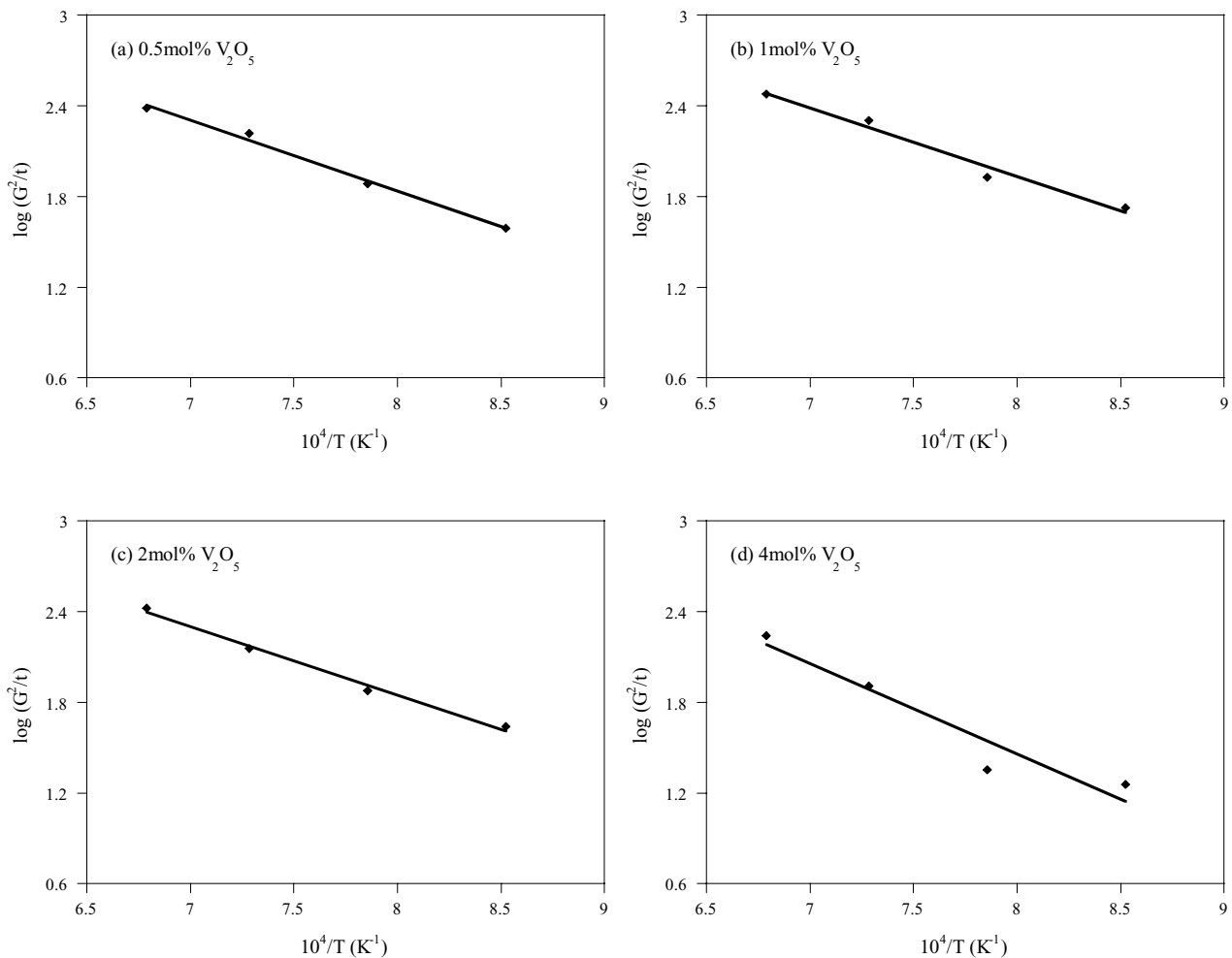


Figure 5 Arrhenius plots for grain growth of ZnO-V<sub>2</sub>O<sub>5</sub> ceramics: (a) 0.5 mol% V<sub>2</sub>O<sub>5</sub>, (b) 1 mol% V<sub>2</sub>O<sub>5</sub>, (c) 2 mol% V<sub>2</sub>O<sub>5</sub>, and (d) 4 mol% V<sub>2</sub>O<sub>5</sub>.

changes to grain boundary controlled when V<sub>2</sub>O<sub>5</sub> addition is further increased to 4 mol%. It is also worth noting that  $Q$  values for all the ZnO-V<sub>2</sub>O<sub>5</sub> systems are lower than that for pure ZnO [21] and ZnO-Bi<sub>2</sub>O<sub>3</sub> systems [21, 22]. This indicates that a faster grain growth rate is achieved with V<sub>2</sub>O<sub>5</sub> doping.

## 5. Conclusion

Grain growth behaviour of ZnO during liquid phase sintering of binary ZnO-V<sub>2</sub>O<sub>5</sub> ceramics with 0.5 to 4 mol% V<sub>2</sub>O<sub>5</sub> has been systematically studied. The ZnO grain size increases as V<sub>2</sub>O<sub>5</sub> content is increased up to 2 mol%. Subsequent increase in V<sub>2</sub>O<sub>5</sub> content causes a reduction in the grain size. The kinetic grain growth exponent  $n$  varies with V<sub>2</sub>O<sub>5</sub> content and ranges from 1.52 to 2.69.  $Q$  values decrease significantly for V<sub>2</sub>O<sub>5</sub>-doped ZnO as compared to pure ZnO. For the range of 0.5–2 mol% V<sub>2</sub>O<sub>5</sub>,  $Q$  and  $K_0$  remains rather constant. Further addition of V<sub>2</sub>O<sub>5</sub> increases both  $Q$  and  $K_0$  values. These results show that mechanism for ZnO grain growth changes with V<sub>2</sub>O<sub>5</sub> content. It is postulated that the mechanism changes from solid-state diffusion of Zn<sup>2+</sup> within the lattice for pure ZnO, to solution-precipitation liquid phase sintering for V<sub>2</sub>O<sub>5</sub>-doped ZnO. For 0.5–2 mol% of V<sub>2</sub>O<sub>5</sub>, the reaction is grain boundary controlled solution-precipitation, whereby grain growth is independent of the thickness of liquid layer. It changes to diffusion through intergranu-

lar liquid layer as V<sub>2</sub>O<sub>5</sub> addition increases to 4 mol%, in which grain growth is liquid thickness dependent.

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